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This is a brief summary of the methods used in TOPPCAT

## T1 Map Sub:

The general equation for signal intensity at a given flip angle  $S(\alpha) = S_0(1 - e^{-TR/T1})\sin(\alpha)/(1 - \cos(\alpha)e^{-TR/T1})$ , where TR is the repetition time,  $\alpha$  is the flip angle, and  $S_0$  is the equilibrium longitudinal magnetization, can be rewritten as  $S(\alpha)/\sin(\alpha) = mS(\alpha)/\tan(\alpha) + S_0(1 - m)$ , where  $m = e^{-TR/T1}$ . For each pixel location, the plug-in performs a linear least-squares fit for the slope  $m$  and the intercept  $S_0(1 - m)$ , considering  $S(\alpha)/\tan(\alpha)$  as abscissa and  $S(\alpha)/\sin(\alpha)$  as ordinate for each flip angle acquired, then solves for T1 and  $S_0$  [1]. This method has been shown to be efficient and reasonably accurate in a recent evaluation [2].

## Start Patlak:

In the first step, the plug-in calculates the T1 relaxation rate  $R1(t)$  at each pixel over time from changes in the signal intensity relative to baseline ( $S(t)-S(0)$ ) using the formula

$$R1(t) = -1/TR \ln \frac{1 - \left( \frac{S(t) - S(0)}{S_0 \sin \alpha} + \frac{1 - m}{1 - (m \cdot \cos \alpha)} \right)}{1 - \cos \alpha \left( \frac{S(t) - S(0)}{S_0 \sin \alpha} + \frac{1 - m}{1 - (m \cdot \cos \alpha)} \right)}$$

(adapted from [3]) where  $\alpha$  and TR are the flip angle and repetition time of the dynamic MR sequence. The user provides both  $S_0$  and T1 maps, with  $m$  calculated as above from the latter. The baseline relaxation rate  $R1(0)$  is calculated by averaging the dynamic images obtained before contrast arrival, and the concentration of gadolinium is calculated from the change in R1:  $C(t) = (R1(t) - R1(0))/\mathfrak{K}1$ , where  $\mathfrak{K}1$  is  $4.39 \text{ s}^{-1}\text{mM}^{-1}$  for gadolinium [3].

In the second step,  $K^{\text{trans}}$  and vascular volume maps are calculated using Patlak analysis. Patlak analysis is a relative simple method that attempts to separate contrast agent distribution due to permeability effects from those due to increased vascularity [4].  $K^{\text{trans}}$  of gadolinium derived using this method have correlated well with  $^{14}\text{C}$ -sucrose transfer constants in a model of rat cerebral ischemia [5]. The equation for the Tofts-Kermode model [4] for contrast agent distribution modified [6] to take into account the presence of separate extracellular and intravascular compartments is

$$C_t(t) = K^{\text{trans}} \int_0^t C_p(\tau) e^{-\frac{K^{\text{trans}}}{v_e}(t-\tau)} d\tau + v_p \cdot C_p(t)$$

where  $v_e$  is the fractional volume of the extracellular extravascular volume,  $C_t(t)$  is the tissue concentration over time, and  $C_p(t)$  is the plasma concentration over time. Patlak analysis assumes that the value of the exponential term is unity because either the back diffusion rate  $K^{\text{trans}}/v_e$  is small,  $t-\tau$  is small, or both. If this is the case, division of the entire equation by  $C_p(t)$  yields a linear equation, if  $\int C_p(\tau)d\tau/C_p(t)$  is considered the ordinate and  $C_t(t)/C_p(t)$  is considered the abscissa for each time point. The plug-in uses the least squares method to solve this equation for the slope  $K^{\text{trans}}$  and the intercept  $v_p$ . A concentration time curve chosen from a region of interest in a vascular structure, adjusted for capillary hematocrit (user-supplied), is used as a surrogate for  $C_p(t)$ .

#### References:

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